| Algorithm Name | Video on ECS60 Site | $\begin{array}{\|l} \hline \mathrm{Dv}= \\ \text { distance to vertex } \end{array}$ | ADT | Notes | Sample uses | General Steps | Big-Oh explanation |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Critical Path <br> Analysis Using <br> Topological Sort | Video: 11-09 <br> Time: 08:00 | n/a | Queue | For graphs that are weighted, directed and acyclic. Schedule, dependency. | Building a house has many steps. Some tasks can be done simultaneously and some depend on others being done. Determine what tasks are most critical to do. | 1. Convert Activity Node Graph (weighted verticies) to Event Node Graph (weighted edges) <br> 2. Use Topological sort ( $\mathrm{O}(\mathrm{V}+\mathrm{E}$ ) which is very fast) to determine CRITICAL PATH <br> 3. Go left to right to determine EARLIEST START times <br> 4. Go right to left to determine LATEST COMPLETION times | $\mathrm{O}(\mathrm{V}+\mathrm{E})$ |
| Unweighted Shortest Path | Video 11-09 <br> Time: 30:25 | 1 + DISTw | Queue | For unweighted graphs (unbeatably fast big-Oh) <br> Similar to level-order-traversal but done on a graph | Manhattan distances where all edges are the same | 1. Use three column table: verticies, pv and dv <br> 2. Start at distinguished vertex, get adjacent verticies, add to queue | $O(V+E)$ <br> because you are putting each vertex into the queue and are looking at every edge |
| Articulation Points | Video: 11-18 <br> Time: 14:00 | n/a | Stack of recursion | if a graph is not bi-connected, the verticies whose removal would disconnect the graph are Articulation Points. | A problem with bridges that act as bottlenecks | 1. Pick starting vertex <br> 2. Number verticies using DFS <br> 3. low min: <br> a. num(v) <br> b. lowest low of children of $v$ <br> c. num of a backedge of $v$ | $\mathrm{O}(\mathrm{V}+\mathrm{E})$ |
| Dijkstra's | Video: 11-09 <br> Time: 28:40 (he then talks about Breadth First Search so can skip to 36:00) <br> Video: 11-13 <br> Time: 13:00 | COSTvw + DISTw cost of edge from $v$ to $w$ + distance to w (cumulative) | Min Heap, Min Heap w/Hash, or None. | For weighted graphs <br> Shortest path: Given a distinguished vertex (so different from MST) and want to determine minimum path to all other verticies <br> Cumulative is key <br> - uses a min heap | There are a bunch of connected train stations and train cars scattered at the stations that need to go to a different station. You need to determine the best way to pick up and deliver the cars to their destinations. | 1. Use four column table: verticies, known, pv and dv 2. Start at distinguished vertex, update adjacent verticies | $\mathrm{O}\left(\mathrm{V}^{\wedge} 2\right)$ using no ADT for dense graphs because $E \log E$ for a dense graph is ( $\left.v^{\wedge} 2\right) / 2 \log \left(v^{\wedge} 2\right) / 2$ which is worse. O(E Log E) using heap. O(E Log V) technically 2(E $\log \mathrm{V}$ ) using heap w/hash |
| Prim's | Video: 11-13 <br> Time: 36:30 | COSTvw cost of edge from $v$ to $w$ (non-cumulative) | Same as Dijkstras | - Builds MST (note that MST uses an arbitrary starting vertex, unlike Dijkstra which is used for shortest path so uses a distinguished vertex) <br> -Greedy Algorithm - same as Dijkstra's except noncumulative | You want to make a network of computers so which paths do you choose so that your network has minimum of materials being used? | 1. Choose ARBITRARY vertex <br> 2. Select closest vertex |  |
| Kruskal's | Video: 11-16 <br> Time: 06:00 | n/a | Find Union | - Build disjoint sets of MST and combine them. <br> - Choose either Kruskal or Prim's based on Big-Oh |  | 1. Sort all edges by weights from low to high <br> 2. Choose union by height or union by size <br> 3. Accept or reject <br> 4. stop when V - 1 edges completed | O(E $\log \mathrm{E})$ <br> because it is $\mathrm{O}(\mathrm{E} \log \mathrm{V})$ to accept and reject all edges <br> and $\mathrm{O}(\mathrm{E} \log \mathrm{E})$ to sort all edges |
| NetWork Flow (Ford-Fulkerson) | Video: 11-16 <br> Time: 28:30 | minimum(Cvw, Dw) minimum of capacity of edges from $v$ to $w$ and the flow that was into $w$ itself | Max Heap, Max Heap w/Hash, or None. | - Greedy Algorithm but self correcting - Dijkstra-esque but uses a max heap instead of a min heap because we want maximum flow | You have a network of pipes and you want to know the max amount of water that can flow from the source to the sink | 1. Use Dijkstra table with max heap to find augmented path with max flow <br> 2. Done when sink is true | max flow * dijkstra big-oh |

